



**LATVIJAS  
UNIVERSITĀTE**

ANNO 1919

# Elektronu pāru skaldīšana nanoelektroniskajā "kvantu paātrinātājā"

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LZA koresp. loceklis

Ziņojums Latvijas Zinātņu Akadēmijā  
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# Partitioning of on-demand electron pairs

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1. Eksperiments veikts Hanoverē



Leibniz  
Universität  
Hannover

1. Ierīce radīta Braunšveigā

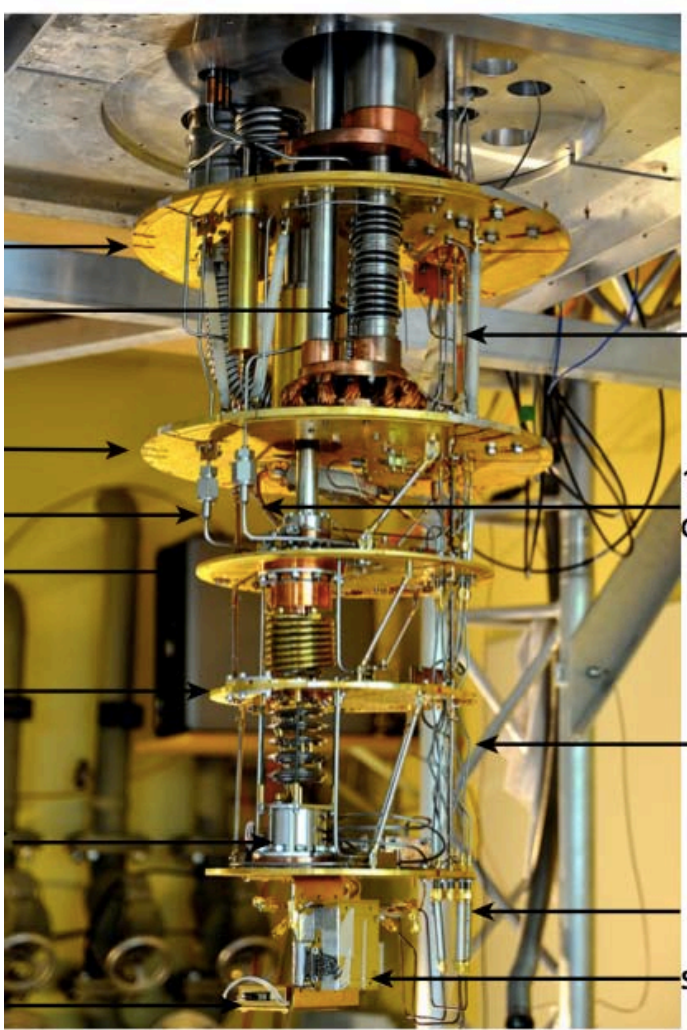


Physikalisch  
Technische  
Bundesanstalt  
Braunschweig und Berlin

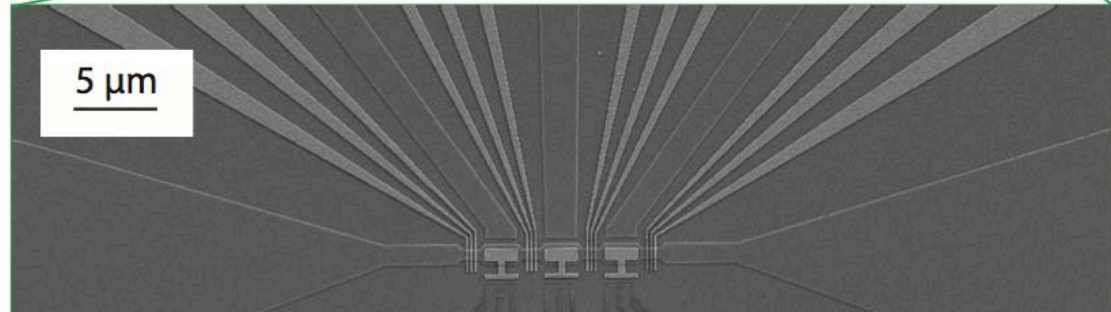
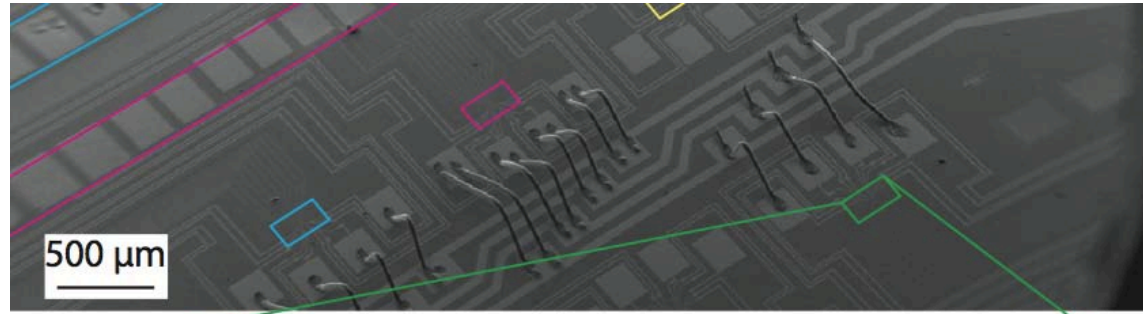
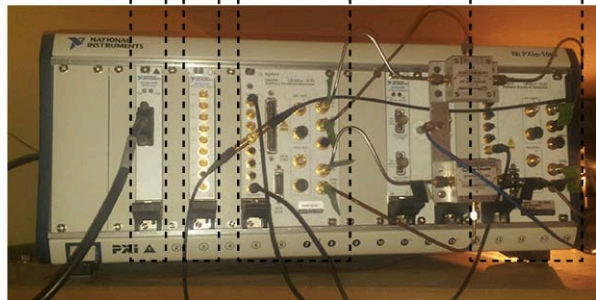
1. Teorija izstrādāta Rīgā



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8-channel PCIe bus      2-channel digitizer AWG (master)      2-channel AWG (slave)



For a specific model calculation we consider a sudden onset of strong dot-lead coupling in a quantum-impurity-like model of the quantum dot and edge channel, governed at  $t > 0$  by the Hamiltonian

$$\mathcal{H} = \varepsilon_c(d_1^\dagger d_1 + d_2^\dagger d_2) + (\Delta\varepsilon + U d_1^\dagger d_1) d_2^\dagger d_2 \quad (S5)$$

$$+ \sum_{i=1,2} \sqrt{\gamma_i/(2\pi\nu)} \sum_k (d_i^\dagger c_k + c_k^\dagger d_i) + \sum_k \varepsilon_k v_F c_k^\dagger c_k. \quad (S6)$$

Here  $\varepsilon_c > E_b$  is the lowest single-electron energy level right after application of the emission pulse at  $t = 0$ ;  $\nu$  is the density of states in the lead with a quasi-continuous spectrum  $\varepsilon_k$ .  $d_1$ ,  $d_2$  and  $c_k$  are the usual fermionic annihilation operators for a single spin species. The level broadenings  $\gamma_1$ ,  $\gamma_2$  are on the order of  $\hbar\Gamma_b$  which in turn is expected to be on the order of level-spacing  $\Delta\varepsilon$ . Pre-emission Coulomb charging energy is described by the Hubbard parameter  $U$ .

Starting from initial conditions at  $t = 0$  with two electrons on the dot,  $\langle d_1^\dagger d_1 \rangle + \langle d_2^\dagger d_2 \rangle = 2$ , and a drained Fermi sea,  $\langle c_k^\dagger c_q \rangle = 0$ , time evolution of the two-particle wavefunction governed by Eq. (S6) can be solved exactly using standard methods. For  $t \gg \Gamma_b^{-1}$ , the solution converges to  $|\Psi\rangle = \sum_{k,q} \psi_{kq} |k\rangle \otimes |q\rangle$  where  $\psi_{kq} = -\psi_{qk}$  and  $|k\rangle$  are the single particle states in the lead created by  $c_k^\dagger$ . The asymptotic two-particle amplitudes are

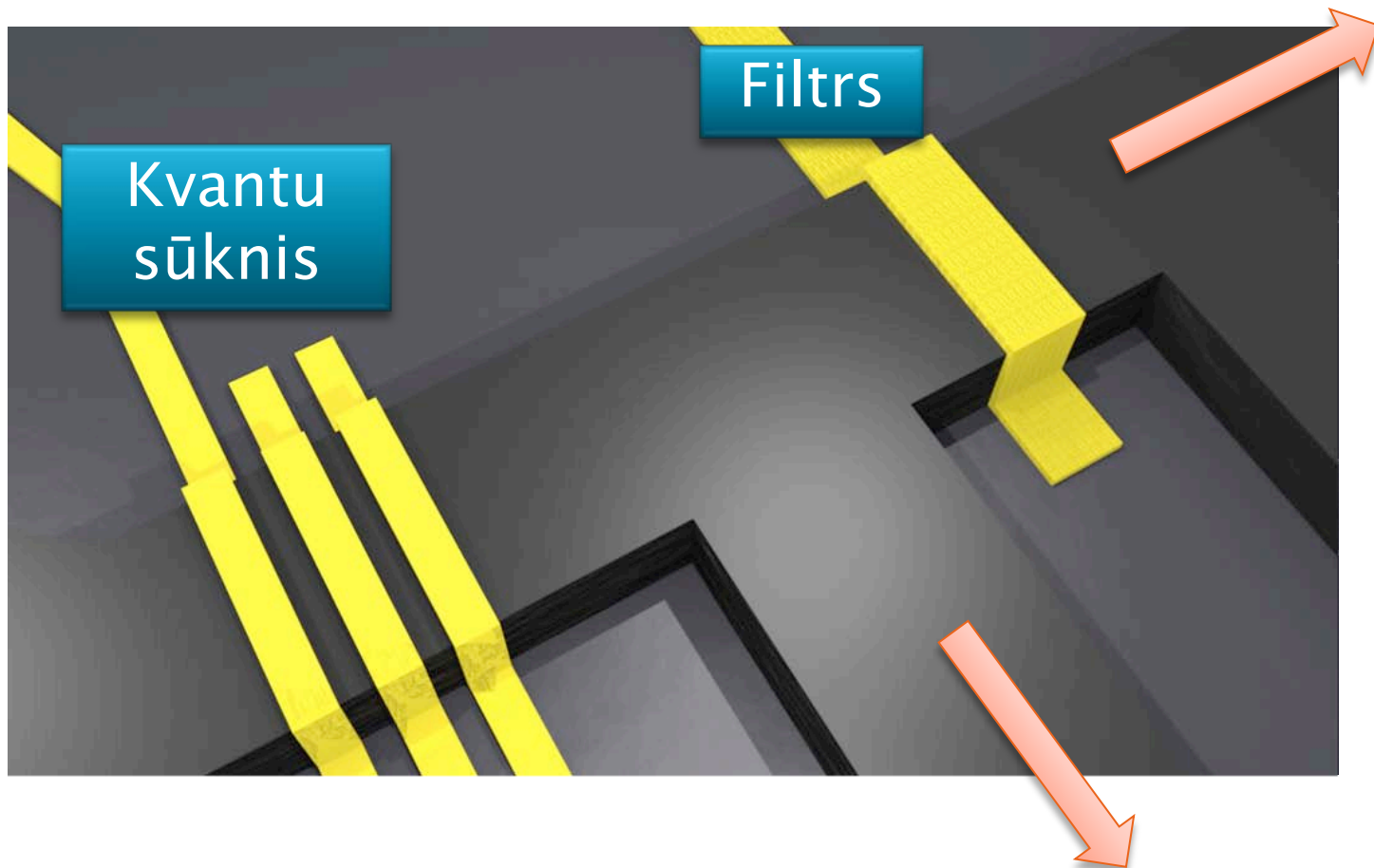
$$\psi_{kq} = \frac{1}{2\pi\nu\sqrt{2}} \frac{\Delta\varepsilon \sqrt{\gamma_1\gamma_2}}{(\varepsilon_q - z_1)(\varepsilon_q - z_2)(\varepsilon_q + \varepsilon_k - U - z_1 - z_2)} - (q \leftrightarrow k). \quad (S7)$$

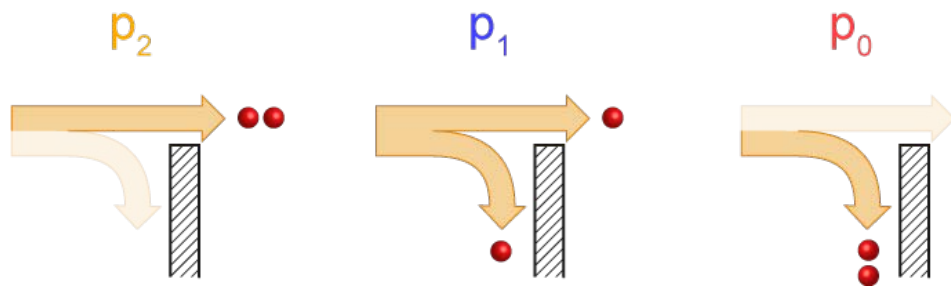
Here  $z_1$  and  $z_2$  are the (complex) roots of the secular quadratic equation:  $(z - z_1)(z - z_2) = (z - \varepsilon_c + i\gamma_1/2)(z - \varepsilon_c - \Delta\varepsilon + i\gamma_2/2) + \gamma_1\gamma_2/4$ .

For  $\gamma_1 = \gamma_2 = \Delta\varepsilon$  (which mimics ballistic propagation over the exit barrier), the joint probability distribution to find one electron at energy  $\varepsilon_k$  and the other at  $\varepsilon_q$  is

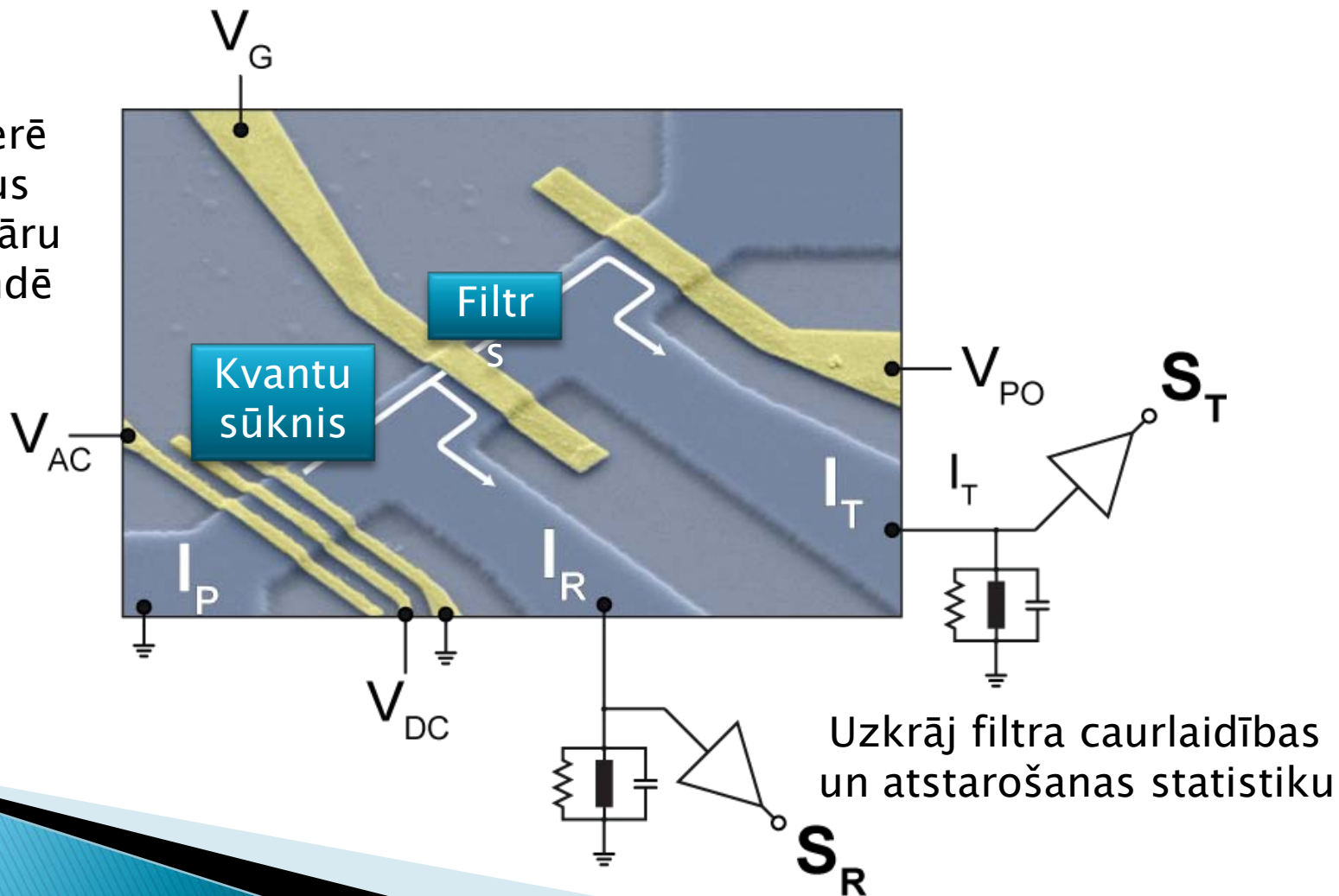
$$\nu^2 |\psi_{kq}|^2 = \frac{\Delta\varepsilon^4}{8\pi^2} \frac{(\varepsilon_k - \varepsilon_q)^2 [(\varepsilon_k + \varepsilon_q)^2 + \Delta\varepsilon^2]}{(\varepsilon_k^2 + \Delta\varepsilon^2/4)(\varepsilon_q^2 + \Delta\varepsilon^2/4)[(\varepsilon_k + \varepsilon_q - U)^2 + \Delta\varepsilon^2]} \quad (S8)$$

This result contains both fermionic ( $\psi_{kk} = 0$ ) and interactions-induced (for  $U > 0$ ) correlations. We plot the projected

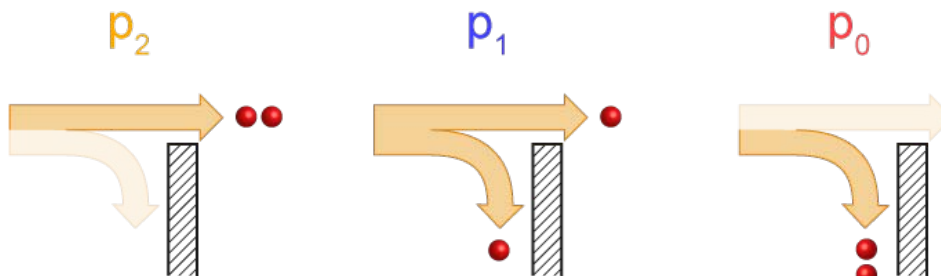
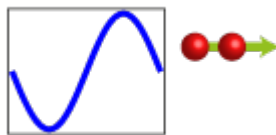




Sūknis ģenerē  
240 miljonus  
elektronu pāru  
vienā sekundē



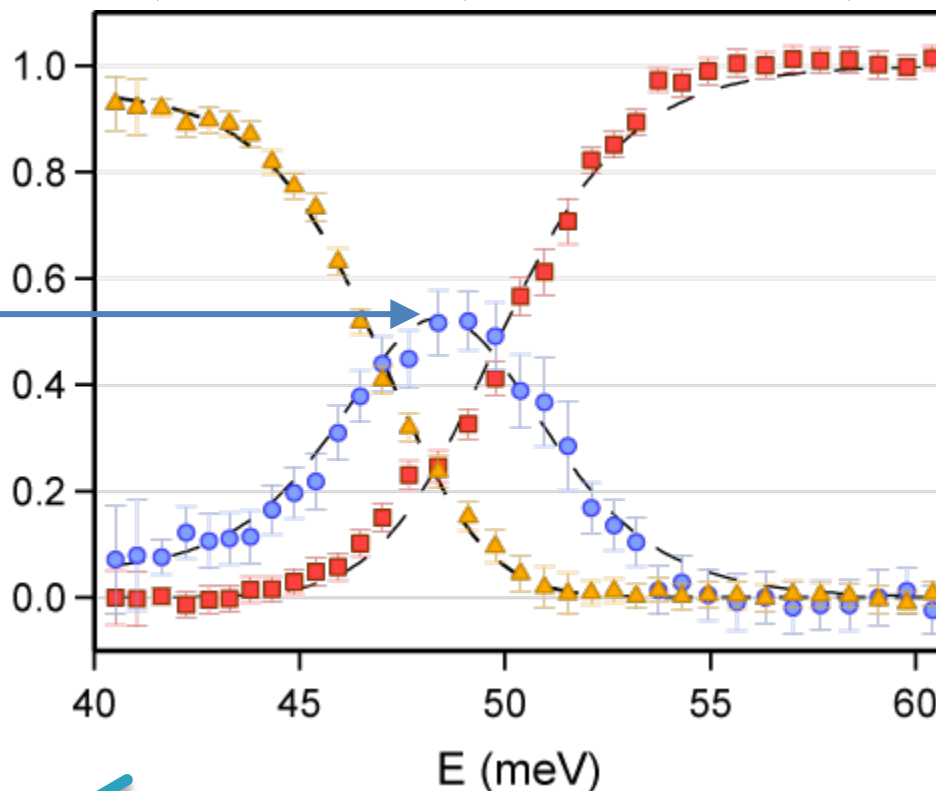
# Divi elektroni secīgi



Binomiālā  
statistika



50%

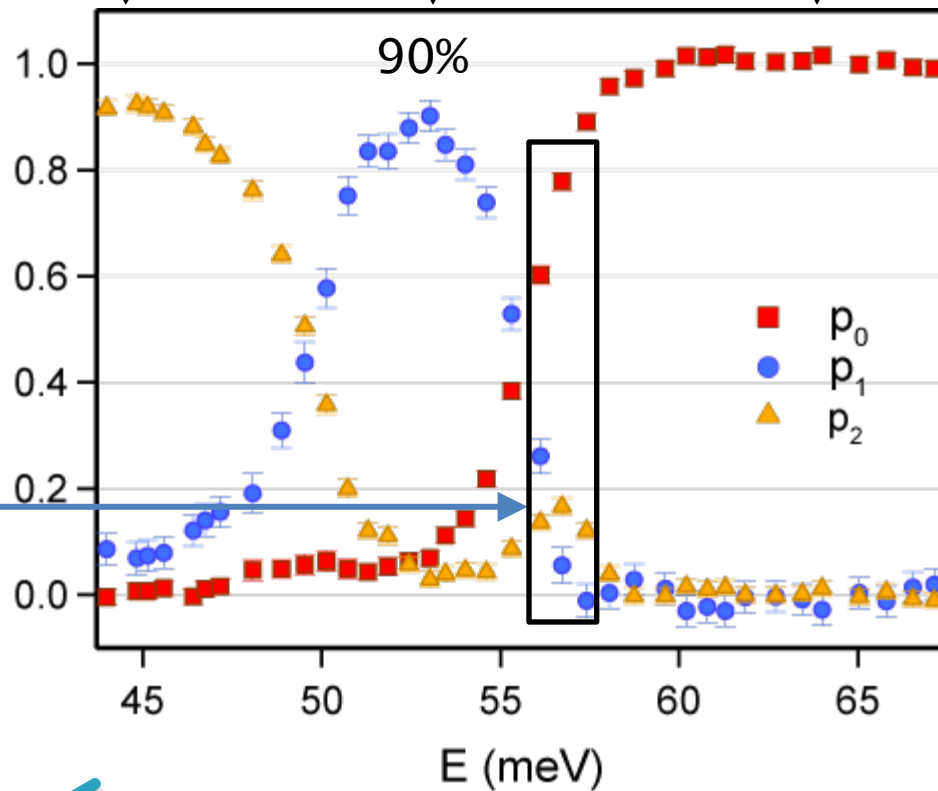
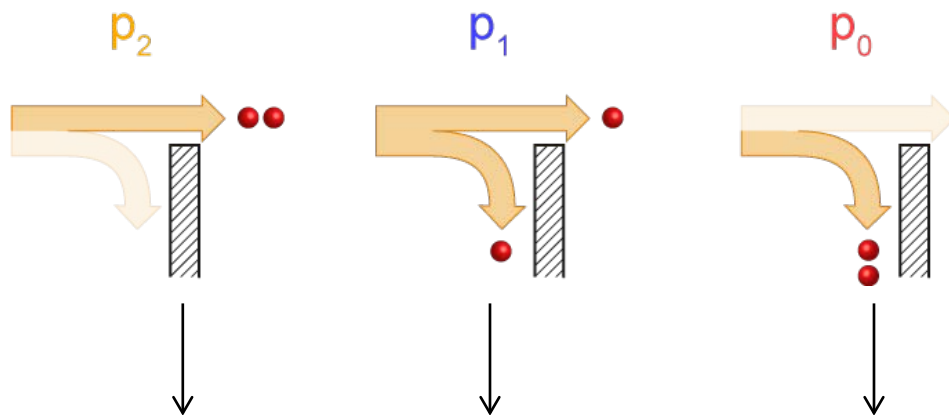


Filtra caurlaidība

# Divi elektroni vienlaicīgi



Anomāla korelācija  
(saistība) !

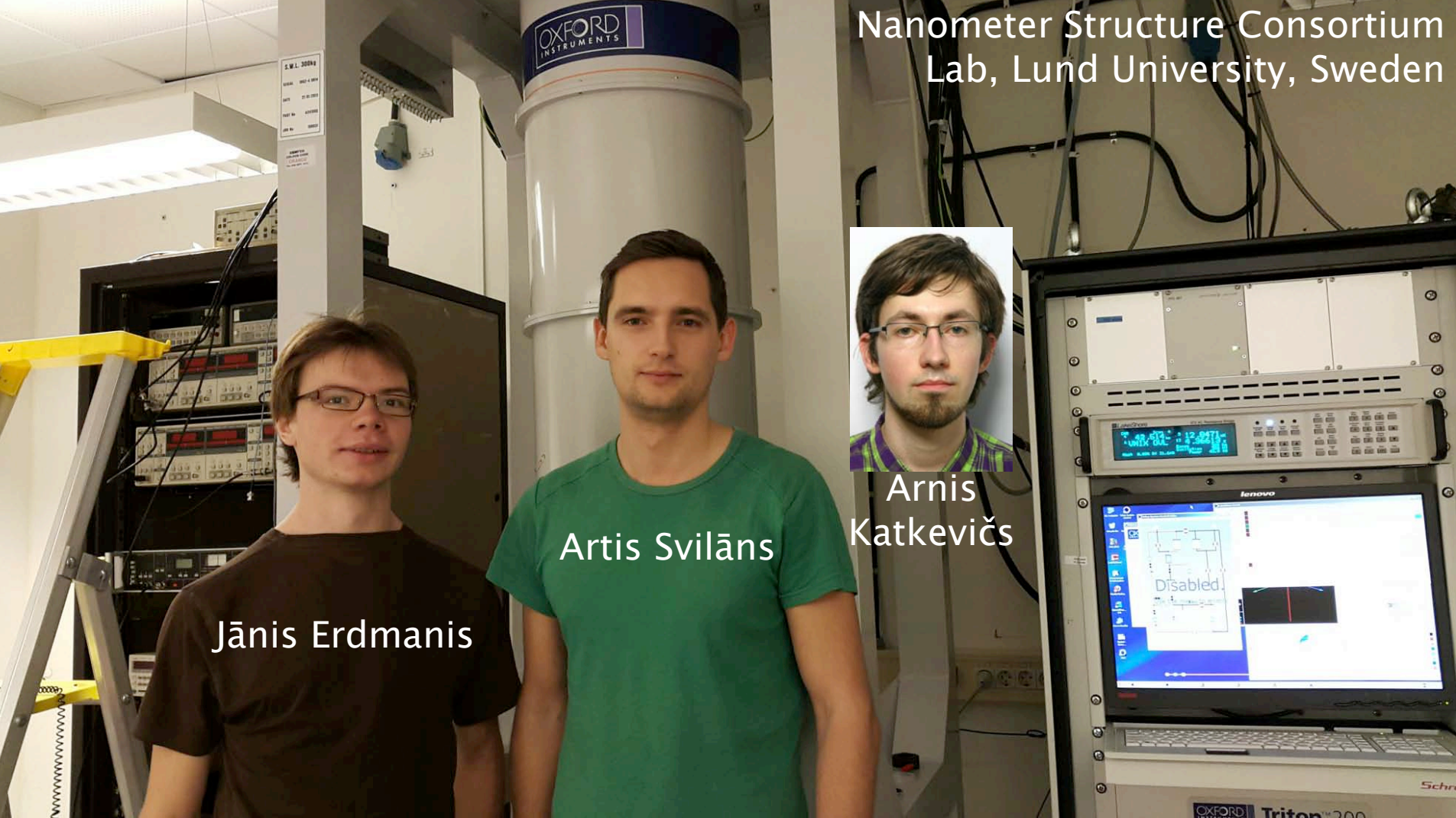


Filtra caurlaidība

# Secinājumi

- ▶ Demonstrēta augstas precizitātes atsevišķu elektronu “balistiskā stūrēšana”
- ▶ Elektronu kvantu optikā “staru dalītājs” ir nelineārs elements
- ▶ Novērotā “skaldīšanas statistikas” anomālija ir pretrunā ar līdz šīm zināmām teorijām
- ▶ Nākamais solis – kvantu interference nanoshēmā atsevišķu elektronu līmenī!





Jānis Erdmanis

Artis Svilāns

Arnis  
Katkevičs

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*Nelīdzsvara kvantu statistika elektroniskajās nanoierīcēs*